

## Fonctions angulaires

$$\begin{aligned}
Y_0^0 &= \left(\frac{1}{4\pi}\right)^{1/2} \\
Y_1^0 &= \left(\frac{3}{4\pi}\right)^{1/2} \cos(\theta) \\
Y_1^{\pm 1} &= \mp \left(\frac{3}{8\pi}\right)^{1/2} \sin(\theta) e^{\pm i\phi} \\
Y_2^0 &= \left(\frac{5}{16\pi}\right)^{1/2} (3\cos^2(\theta) - 1) \\
Y_2^{\pm 1} &= \mp \left(\frac{15}{8\pi}\right)^{1/2} \sin(\theta) \cos(\theta) e^{\pm i\phi} \\
Y_2^{\pm 2} &= \left(\frac{15}{32\pi}\right)^{1/2} \sin^2(\theta) e^{\pm 2i\phi} \\
Y_3^0 &= \left(\frac{7}{16\pi}\right)^{1/2} (5\cos^3(\theta) - 3\cos(\theta)) \\
Y_3^{\pm 1} &= \mp \left(\frac{21}{64\pi}\right)^{1/2} \sin(\theta) (5\cos^2(\theta) - 1) e^{\pm i\phi} \\
Y_3^{\pm 2} &= \left(\frac{105}{32\pi}\right)^{1/2} \sin^2(\theta) \cos(\theta) e^{\pm 2i\phi} \\
Y_3^{\pm 3} &= \mp \left(\frac{35}{64\pi}\right)^{1/2} \sin^3(\theta) e^{\pm 3i\phi}
\end{aligned}$$

## Fonctions radiales

$$\begin{aligned}
R_{10} &= 2a^{-3/2} e^{-r/a} \\
R_{20} &= \frac{1}{\sqrt{2}} a^{-3/2} \left(1 - \frac{1}{2} \frac{r}{a}\right) e^{-r/2a} \\
R_{21} &= \frac{1}{\sqrt{24}} a^{-3/2} \frac{r}{a} e^{-r/2a} \\
R_{30} &= \frac{2}{\sqrt{27}} a^{-3/2} \left(1 - \frac{2}{3} \frac{r}{a} + \frac{2}{27} \left(\frac{r}{a}\right)^2\right) e^{-r/3a} \\
R_{31} &= \frac{8}{27\sqrt{6}} a^{-3/2} \left(1 - \frac{1}{6} \frac{r}{a}\right) \left(\frac{r}{a}\right) e^{-r/3a} \\
R_{32} &= \frac{4}{81\sqrt{30}} a^{-3/2} \left(\frac{r}{a}\right)^2 e^{-r/3a} \\
R_{40} &= \frac{1}{4} a^{-3/2} \left(1 - \frac{3}{4} \frac{r}{a} + \frac{1}{8} \left(\frac{r}{a}\right)^2 - \frac{1}{192} \left(\frac{r}{a}\right)^3\right) e^{-r/4a} \\
R_{41} &= \frac{\sqrt{5}}{16\sqrt{3}} a^{-3/2} \left(1 - \frac{1}{4} \frac{r}{a} + \frac{1}{80} \left(\frac{r}{a}\right)^2\right) \frac{r}{a} e^{-r/4a} \\
R_{42} &= \frac{1}{64\sqrt{5}} a^{-3/2} \left(1 - \frac{1}{12} \frac{r}{a}\right) \left(\frac{r}{a}\right)^2 e^{-r/4a} \\
R_{43} &= \frac{1}{768\sqrt{35}} a^{-3/2} \left(\frac{r}{a}\right)^3 e^{-r/4a}
\end{aligned}$$

**Matrices de Pauli**

$$\sigma_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \sigma_y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} \sigma_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$